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# MODELLING GTHA POST- SECONDARY SCHOOL LOCATION CHOICE

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## 1 Introduction

The purpose of this investigation is to develop an effective school location choice model for post-secondary (PS) students in the Greater Toronto-Hamilton Area (GTHA). Section 2 presents a brief literature review on relevant works in PS school location choice modelling in general, and in the GTHA specifically; Section 3 then identifies how the contributions of this study differ from the conventional literature in the field. Section 4 introduces the two modelling methods used in this study: random utility models and random forest models. Section 5 then describes the two datasets used: the 2015 and 2019 StudentMoveTO (SMTO) surveys. Sections 6 and 7 then present a detailed modelling exercise using the 2015 dataset, using random utility (Section 6) and random forest (Section 7) methods; Section 8 summarizes and discusses the main results for the 2015 modelling. Building on the 2015 analysis, Section 9 repeats the random utility modelling exercise using the 2019 data, with Section 10 summarizing the key findings from this analysis. Finally, Section 11 concludes the report with a brief discussion of possible directions for future work.

## 2 Literature Review

This section presents a brief review of the PS school choice literature (Section 2.1) and previous work on this problem in the GTHA (Section 2.2). With the exception of the GTHA-based work, it appears that PS school choice has not been well-studied in Canada, with the vast majority of the research to date occurring in the U.S.

### 2.1 Post-Secondary (PS) School Choice Modelling

From a conceptual point of view, frameworks for the PS school choice model have been presented by [Perna](#) (2006) and [Acevedo-Gil](#) (2017). In empirical practice, the most common approach to model this choice is using a multinomial logit model (MNL), or variants thereof. However, other techniques can be used, such as a regression analysis as implemented by [Hearn](#) (1984). In this study, higher test scores, educational aspirations, parental income and academic achievement were found to be most correlated with higher selectivity, while belonging to certain ethnic and gender groups had negative effects on college selectivity. These results confirm previous findings of what Hearn calls “nonmeritocratic tendencies” in the American college choice system.

Such “nonmeritocratic tendencies” are observed in other studies as well. Specifically, [Niu et al.](#) (2006) find, in an analysis of college choices of Texas students, that Black and Hispanic students are less likely to enrol in more selective institutions (except for the most selective group), while the opposite pattern applies to Asian students. On the other hand, [Montgomery](#) (2002) uses a nested logit (NL) model to analyze choice of graduate business school and enrollment status (full-time or part-time) in the United States and finds that minorities and males are more responsive to school reputation, exhibiting a stronger preference for higher-reputation institutions. It is unclear to what extent such tendencies exist in the GTHA.

Another common observation found by [Montgomery](#) (2002) is that greater distance from home reduces the attractiveness of an institution. [Kohn et al.](#) (1974) make this observation after implementing conditional logit models for PS school choice in Illinois and North Carolina. [Oosterbeek et al.](#) (1992) also notice this pattern when using an MNL model to analyze data on university choices of Dutch economists. [Long](#) (2004) uses a conditional logit model to analyze

changes in PS school decisions over time and finds that distance from home negatively impacts the probability of attending a school. Interestingly, they note that this effect has decreased over time.

Finally, many studies show relationships between certain campus attributes and their perceived utilities. For instance, higher tuition fees are normally connected with lower utilities. [Kohn et al.](#) (1974) find that the disutility due to greater tuition fees is smaller for higher-income groups in particular. [Long](#) (2004) finds that students in 1992 consider institution quality and selectivity to be a more important factor than students in 1972 and 1982, and that higher tuition reduces college's perceived utilities. [Sá et al.](#) (2012) use an NL model to predict living arrangement and university choice for Dutch post-secondary students, while [Niu and Tienda](#) (2007) analyze PS school choice in Texas, and specifically investigate the effects of constraining choice sets in different ways. In both studies, institutional attributes such as quality and selectivity are used to model the base utility of each school.

## 2.2 PS School Location Choice in the GTHA

StudentMoveTO (n.d.) publishes a list of works which make use of the survey data. Many of these works analyze students' commute patterns, including mode choice, and bike or license ownership. [Chung et al.](#) (2018) analyze living arrangement decisions for students at the University of Toronto. However, no published works as of yet have developed a school location choice model based on the StudentMoveTO (SMTO) data.

Past researchers from the University of Toronto's [Travel Modelling Group](#) have investigated school location choice models for the GTHA. [Chen](#) (2018) estimates a doubly-constrained gravity model using data from the 2016 [Transportation Tomorrow Survey](#) (TTS). While this model was effective for students at the elementary and secondary levels, it was found to be ineffective for the post-secondary level. [Wang](#) (2015) estimates another doubly-constrained gravity model with an accessibility model for the utility term using data from the 2011 TTS. Likewise, this model was found to be ineffective for both full-time and part-time post-secondary students. Both these findings provide motivation for a more advanced post-secondary school location choice model to be developed.

## 3 Contributions

This analysis differs from previous works PS school choice modelling on several fronts.

Firstly, this model is not representing the college choice process directly. Instead, this analysis is an exercise in matching students who have already made PS school choice decisions to their selected institutions. While there are many areas of overlap, an important difference is that household information reflects where students reside after having selected a college, and possibly, moving out from their parental homes.

Secondly, this study primarily analyzes geographical patterns in school location choice for applications in travel demand modelling. An emphasis is placed on modelling the accessibility of each school location to each student, rather than predicting school selectivity or institution type.

Thirdly, an RF classifier is implemented for the location choice problem, a novel approach in the field, and its utility is compared to that of the classic econometric approaches.

## 4 Methods

### 4.1 Random Utility Models

As indicated in the literature review, the multinomial logit model (MNL) is the most common method used to model PS choice. The model is derived within a random utility framework by [McFadden \(1973\)](#), and described in depth by [Train \(2003\)](#). The perceived utility of alternative  $j$  for student  $i$  is assumed to be  $U_{ij} = V_{ij} + \epsilon_{ij}$ , where  $V_{ij}$  is the systematic utility of location  $j$  for student  $i$  and  $\epsilon_{ij}$  is an associated random utility. A student selects alternative  $k$  if and only if  $U_{ik} > U_{ij} \forall j \neq k$ . The MNL is obtained by assuming that the random utility terms are independent and identically distributed with a Type-1 extreme value distribution. In this formulation, the probability of alternative  $k$  being chosen by individual  $i$  from choice set  $C$  is:

$$P(y_i = k) = \frac{e^{V_{ik}}}{\sum_{j \in C} e^{V_{ij}}} \quad [1]$$

One property of MNL models is that it is consistent with the Independence from Irrelevant Alternatives (IIA) assumption. Namely, this is the property that the probability of alternative  $j$  being selected over alternative  $k$  is independent of the other alternatives in the choice set. When this assumption does not hold, an extension of the MNL model, known as the nested logit (NL) model, can be used ([Ben-Akiva and Bierlaire 1999](#)). In this model, each alternative is placed into one nest, and it is assumed that the error terms in the utilities for the alternatives within each nest are correlated. The probability of alternative  $k$  from nest  $l$  including alternatives  $C_l$  being chosen by individual  $i$  from the set of nests  $M$  is:

$$P(y_i = k) = \frac{e^{\mu V_{im}}}{\sum_{m \in M} e^{\mu V_{im}}} \times \frac{e^{\mu_l V_{ik}}}{\sum_{j \in C_l} e^{\mu_l V_{ij}}} \quad [2]$$

Here,  $\mu$  is the scale parameter reflecting the correlation between the random components of the utility of the nests (at the top level of the model) and  $\mu_l$  reflects the correlation among alternatives in nest  $l$  (at the lower level of the model). The term  $\ln \sum_{j \in C_l} e^{\mu_l V_{ij}}$  is known as the logsum or inclusive value of nest  $l$ , and represents the expected maximum utility for the choice of alternatives in the nest. In order for this formulation to be consistent with the random utility maximization framework,  $\mu_l \geq 1 \forall l \in M$ . Note that if all  $\mu_l = 1$  then the nesting structure is degenerate and the model collapses into the standard MNL.

In this study, logit and nested logit models are estimated using mlogit 1.1-0 ([Croissant 2020](#)) with RStudio 1.3.959 and R 4.0.0. In some cases, [Biogeme 3.2.6](#) ([Bierlaire 2020](#)) was used with Python 3.7.6 and Jupyter Notebook 6.0.3.

### 4.2 Random Forest Models

Random forests (RFs) are a machine learning technique that have been successfully applied in various fields, including genetics, clinical medicine, and bioinformatics ([Strobl et al. 2009](#)). Developed by Breiman (2001), the RF training algorithm is developed as follows ([Hastie et al. 2009](#)). For  $b \in \{1, 2, \dots, B\}$ :

- a) Draw a bootstrapped sample from the training data.
- b) Grow a decision tree  $T_b$  using the bootstrapped data by performing the following steps recursively until minimum node size  $n_{min}$  is reached:
  - a. Select  $m$  features from the training data at random

- b. Select the best feature and split-point from the  $m$  features according to some split criterion
- c. Split the node using that feature and split-point

The RF is the set of trees  $\{T_b\}_1^B$ . The prediction for a given input is the majority vote for the predicted output from all trees. Several hyperparameters can be adjusted in this algorithm. They include:

- $B$ , the number of trees
- $n_{min}$ , the minimum size for leaf nodes
- $m$ , the number of features to consider for each split point
- The splitting criteria to be used
- The maximum tree depth

The RF algorithm is implemented using [scikit-learn](#) 0.22.1 with Python 3.7.6 and Jupyter Notebook 6.0.3.

### 4.3 Metrics Reported

Throughout this report, the following metrics are reported. Table 1 lists these metrics and how they are calculated. A few notes:

- The softmax accuracy is generally prioritized over the hardmax accuracy since it reflects the probabilities assigned to correct observations and is less sensitive to the imbalances in the data (a “reasonable” hardmax accuracy can be reached by predicting the largest campus for all students).
- The log likelihood can only be reported if no actual observations are assigned a probability of 0 (as this would yield a log likelihood of negative infinity).
- The McFadden rho-squared can only be reported where alternative-specific coefficients are used, and hence is not used throughout much of this analysis.

Table 1: Summary of Reported Metrics. Note that  $L_0$  is the log-likelihood for the logit model with only alternative-specific constants, as explained in [McFadden](#) (1975).  $p_{ij}$  represents the probability assigned by the model that student  $i$  attends campus  $j$ , and  $y_i$  represents the campus actually attended by student  $i$ .

Metric	Calculation
<b>Hardmax Accuracy</b>	$HA = \sum_{i=1}^n \left( \left( \operatorname{argmax}_j p_{ij} \right) == y_i \right)$
<b>Softmax Accuracy</b>	$SA = \frac{1}{n} \sum_{i=1}^n p_i$
<b>Log Likelihood</b>	$\log(L) = \log \left( \prod_{i=1}^n p_i \right) = \sum_{i=1}^n \log(p_i)$
<b>McFadden Pseudo Rho-Squared</b>	$\rho^2 = 1 - \frac{\log(L)}{\log(L_0)}$

## 5 Data

### 5.1 2015 SMTO

The 2015 SMTO dataset is the primary one used to develop a proposed school location choice model. Seven campuses are included in the survey: three University of Toronto campuses (St. George - SG, Scarborough - SC, and Mississauga - MI), two York University campuses (Keele - YK, and Glendon - YG), Ryerson University - RY, and OCAD University - OC. Observations whose indicated enrollment level was “Other” (as opposed to “UG” or “Grad”) were removed from the sample; these were also the only observations whose enrollment status was indicated as “Other” (as opposed to “FT” or “PT”). Table 2 tabulates important characteristics of this filtered dataset.

Note that to make the model generalizable to TTS data, only TTS-compatible attributes are used in the analysis. The one exception is living arrangement, which is not available in TTS but is used regardless. A gradient-boosting machine to classify student living arrangement given other attributes has been trained for possible use to impute this attribute for TTS records. The model achieves an accuracy of over 90%, and so living arrangement is retained in the list of available attributes.

### 5.2 2019 SMTO

Table 3 presents the summary statistics for the 2019 SMTO data, which includes data from 27 university and college campuses (including those from the 2015 survey).

Table 2: Tabulation of Key Variables in 2015 SMTO Dataset. Family: whether the student’s indicated living arrangement is “Live with family/parents”. For “Income”, Low is < \$60,000. For “Mode”, Active is walk or bicycle.

		MI	OC	RY	SC	SG	YG	YK	Total	Share
Count	Total	930	455	2708	1074	5912	315	3084	14478	100.0%
Level	UG	858	403	2420	1018	3571	298	2464	11032	76.2%
	Grad	72	52	288	56	2341	17	620	3446	23.8%
Status	FT	893	408	2557	1028	5425	295	2840	13446	92.9%
	PT	37	47	151	46	487	20	244	1032	7.1%
Gender	Female	653	337	1739	745	3860	256	2078	9668	66.8%
	Male	268	105	953	323	2007	56	972	4684	32.4%
	Other	9	13	16	6	45	3	34	126	0.9%
Family	True	666	230	1861	791	2452	205	2014	8219	56.8%
	False	264	225	847	283	3460	110	1070	6259	43.2%
Income	High	139	56	515	159	1000	57	523	2449	16.9%
	Low	172	102	601	240	1425	74	767	3381	23.4%
	Unknown	619	297	1592	675	3487	184	1794	8648	59.7%
Commute Mode	Transit	566	302	2086	697	3139	217	2232	9239	63.8%
	Active	94	138	508	153	2511	41	360	3805	26.3%
	Auto	227	13	105	222	218	52	477	1314	9.1%
	Other	43	2	9	2	44	5	15	120	0.8%
Distance	Mean	15.10	15.16	18.61	13.92	11.25	16.97	17.42	14.63	
	Std. Dev	12.95	15.23	14.12	11.65	12.89	12.62	12.06	13.31	

Table 3: Tabulation of Key Variables in 2019 SMTO Dataset. Family: whether the student's indicated living arrangement is "Live with family/parents". For "Income", Low is < \$90,000. For "Mode", Active is walk or bicycle.

		Uni - UG	Uni - Grad	College	Total	Share
Count	Total	10396	2652	3468	16516	100.0%
Status	FT	10002	2434	3322	15758	95.4%
	PT	394	218	146	758	4.6%
Family	True	4417	558	1081	6056	36.7%
	False	2546	1386	1017	4949	30.0%
	Unknown	3433	708	1370	5511	33.4%
Work	FT	636	421	240	1297	7.9%
	PT	4739	1148	1817	7704	46.6%
	None	5021	1083	1411	7515	45.5%
Income	High	1429	257	156	1842	11.2%
	Low	2527	358	787	3672	22.2%
	Unknown	6440	2037	2525	11002	66.6%
Commute Mode	Transit	4366	1071	1150	6587	39.9%
	Active	1466	638	282	2386	14.4%
	Auto	794	188	551	1533	9.3%
	Other	42	17	13	72	0.4%
	Unknown	3728	738	1472	5938	36.0%
Age	Mean	20.93	27.96	24.60	22.83	
	Std. Dev.	4.87	7.13	7.95	6.59	

## 6 2015 SMTO Location Choice – Logit Model

A number of logit-based models of PS location choice are developed and discussed in this section. They are all estimated using 2015 SMTO data. The models are iteratively developed, beginning with a very simple specification and then more complex specifications are systematically performed, as described in detail in the following sections.

### 6.1 Gravity Model

The first step in the logit model analysis for the 2015 SMTO dataset was estimating simple doubly-constrained gravity models for separate segments in the sample. [Anas \(1983\)](#) shows that the doubly-constrained gravity model is equivalent to MNL with impedance function  $f(d_{ij}) = e^{B_j d_{ij}}$ . Thus, in this study, the utility is specified as  $V_{ij} = B_j + B_{Dist} * d_{ij}$ , where  $B_j$  is known as an alternative-specific constant for alternative  $j$  and  $d_{ij}$  represents the network distance between the student's home zone and each campus. These network distances were obtained from level-of-service matrices generated using the 2016 TTS data and GTAModel V4.1.

The findings from this analysis are presented in Table 4, from which it is seen that there are significant differences between the parameters estimated for the different student groups. In particular, the distance parameter is of greatest magnitude for students not living with their family/parents, and especially so for full-time undergraduates. This result is reasonable as students in this group are likely to be living on residence or to have selected their place of residence according to their place of school (rather than the other way around, as the model implies).

Table 4: Estimation Results for Segmented Gravity Models. UG = Undergrad, G = Grad, FT = Full-time, PT = Part-time, F = Live with family/parents, N = Another living arrangement. \*\*\* indicates  $p < 0.001$ .

Segment	Count	$B_{Dist}$	Std. Error	
UG FT N	3461	-0.16042	0.00378	***
UG FT F	6879	-0.06148	0.00155	***
UG PT N	314	-0.08704	0.00940	***
UG PT F	378	-0.06178	0.00709	***
G FT N	2250	-0.09309	0.00419	***
G FT F	856	-0.05527	0.00729	***
G PT	340	-0.07323	0.01260	***
All	14478	-0.08336	0.00121	***

## 6.2 Accessibility Model

The doubly-constrained gravity model used above uses network distance as a very simple representation of the impedance experienced by each student travelling to each campus. It can be hypothesized that that the model can be significantly improved by including a more robust measure of the accessibility of each school location to each student. For this reason, a mode choice model was estimated, with the intention of including the expected maximum utility from the mode choice model for each alternative as a logsum term in the location choice model, as outlined by [Ben-Akiva and Lerman](#) (1985). As such, the updated utility function is:

$$V_{ij} = B_j + B_{Access} * \log(e^{V_{ijActive}} + e^{V_{ijAuto}} + e^{V_{ijTransit}}) \quad [5]$$

where the utility of any unavailable mode is negative infinity.

### 6.2.1 Basic Mode Choice Model

The mode choice model takes the form of an MNL model with three alternatives: Auto, Transit, and Active Mode (walking or biking). A first, base mode choice model uses the simple utility function:

$$V_{ijm} = B_m + B_{t_m} t_{ijm} \quad [3]$$

where  $t_{ijm}$  is the morning travel time from student  $i$ 's home zone to campus  $j$ , by mode  $m$ , obtained using the same level-of-service matrices as above. Note that the model includes alternative-specific constants ( $B_m$ ) to reproduce aggregate mode shares for mode  $m$  (taking transit as the reference mode), and alternative-specific coefficients for travel time. 120 students whose indicated modes are not one of the three alternatives are removed from the mode choice estimation set. Table 5 lists the results from this base model.

One result to notice is that the time parameters for each mode are significantly different, so alternative-specific coefficients are retained in subsequent models rather than adopting a generic time coefficient.

Table 5: Base Mode Choice Model.  $B_{Transit} = 0$ . Active mode travel times are calculated given speeds of 4km/h. All travel times are in minutes. \*\*\* indicates  $p < 0.001$ .

Parameter	Estimate	Std. Error	
$B_{Active}$	1.960	0.0495	***
$B_{Auto}$	-2.121	0.0640	***
$B_{t_{Transit}}$	-0.0075	0.0008	***
$B_{t_{Auto}}$	-0.0339	0.0007	***
$B_{t_{Active}}$	-0.0165	0.0019	***
Metric	Result	Metric	Result
Hardmax Accuracy	0.822	McFadden R <sup>2</sup>	0.375
Softmax Accuracy	0.706	Log likelihood	-7663.5

### 6.2.2 Socioeconomic Variables in Mode Choice Model

After estimating this base model, the influence of including various individual and household characteristics in the model was tested. Since these characteristics are consistent across all alternatives, alternative-specific coefficients must be used. The variables whose impact is most significant are living arrangement and license ownership. Hence, the updated utility function is

$$V_{ij} = B_j + B_{t_j}t_{ij} + B_{F_j}F_i + B_{L_j}L_i \quad [4]$$

where  $F_i = 1$  if student  $i$  lives with family/parents, 0 otherwise, and

$L_i = 1$  if student  $i$  owns a driver's license, 0 otherwise.

The results for this model are shown in Table 6. As expected, students living with their family and/or owning a driver's license are more likely to drive to school, and less likely to use an active mode.

Table 6: Mode Choice Model with Selected Socioeconomic Variables.  $B_{Transit} = 0$ . Active mode travel times are calculated given speeds of 4km/h. All travel times are in minutes. \*\*\* indicates  $p < 0.001$ .

Parameter	Estimate	Std. Error	
$B_{Active}$	1.878	0.0612	***
$B_{Auto}$	-3.406	0.1043	***
$B_{F_{Active}}$	-1.459	0.0743	***
$B_{F_{Auto}}$	0.323	0.0737	***
$B_{L_{Active}}$	0.350	0.0625	***
$B_{L_{Auto}}$	1.753	0.0857	***
$B_{t_{transit}}$	-0.0070	0.0008	***
$B_{t_{Active}}$	-0.0290	0.0007	***
$B_{t_{Auto}}$	-0.0221	0.0021	***
Metric	Result	Metric	Result
Hardmax Accuracy	0.826	McFadden R <sup>2</sup>	0.418
Softmax Accuracy	0.722	Log likelihood	-7139.5

### 6.2.3 Availability Restrictions in Mode Choice Model

To further refine the mode choice model, choice set restrictions for certain alternatives in certain choice situations are examined. Two types of availability restrictions are considered: for active modes and auto.

Note that some observations may contradict assumptions about mode availability (e.g. a student indicating they drive to campus despite not owning a car). Such “invalid” observations have probability zero in the availability-restricted models, resulting in a log likelihood of negative infinity. For this reason, log likelihood is not used to compare availability-restricted models.

Students are unlikely to use an active mode (walking or cycling) for trips of long distances due to factors such as the associated physical exertion, dangers, and exposure to weather, in addition to the long travel times. Therefore, models were tested in which the active mode alternative is marked as unavailable in cases where the estimated walking travel time is greater than some threshold  $t$ .

Figure 1 shows how the softmax accuracy changes for various walking time thresholds. The optimal accuracy is reached when a threshold of about 46.6 minutes is imposed, yielding a softmax accuracy of 75.04%.

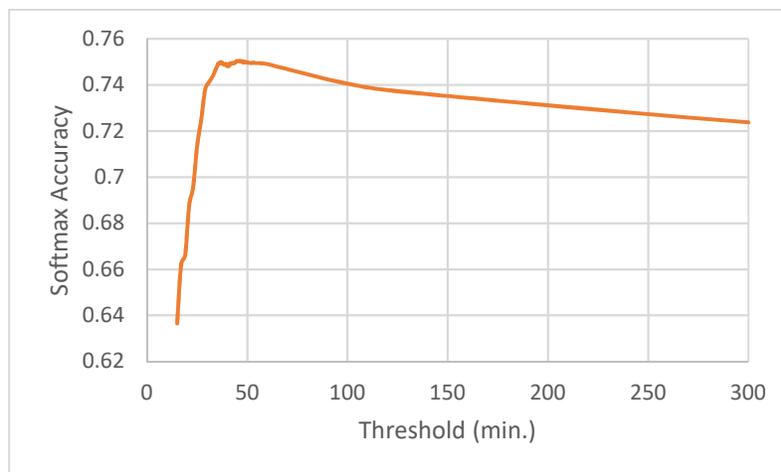


Figure 1: Effect of Travel Time Threshold for Active Mode on Softmax Accuracy.

Students are also unlikely to choose the auto option if there is no vehicle available in their household. As such, models where the auto mode is only available if the student has indicated that their household owns at least  $n$  vehicles, where  $n \in \{0, 1, 2\}$ , are tested. These restrictions are tested both with and without the active mode threshold of 46.6 minutes from above. It is found that setting  $n = 2$  yields the best softmax accuracy in both cases. Note that although license ownership information was available, this information was not used to impose availability restrictions as the Auto mode choice includes students who are auto passengers.

### 6.2.4 Proposed Mode Choice Model

The final mode choice model uses the utility model and optimal availability restrictions described above ( $t_{Active} \leq 46.6$  min. and  $\#Cars \geq 2$ ). Table 7 presents the results for this proposed model, while Tables 8 and 9 show confusion matrices for this model.

Table 7: Proposed Mode Choice Model.  $B_{Transit} = 0$ . Active mode travel times are calculated given speeds of 4km/h. All travel times are in minutes. \*\*\* indicates  $p < 0.001$ . McFadden  $R^2$  and Log likelihood not reported since availability restrictions result in probabilities of 0 assigned to observed choices in some cases.

Parameter	Estimate	Std. Error	
$B_{Active}$	3.890	0.169	***
$B_{Auto}$	-1.696	0.169	***
$B_{F_{Active}}$	-0.992	0.147	***
$B_{F_{Auto}}$	-0.792	0.121	***
$B_{L_{Active}}$	0.613	0.113	***
$B_{L_{Auto}}$	1.622	0.117	***
$B_{t_{Transit}}$	-0.0113	0.001	***
$B_{t_{Active}}$	-0.0936	0.006	***
$B_{t_{Auto}}$	-0.0378	0.003	***
Metric	Result	Metric	Result
Hardmax Accuracy	0.837	McFadden $R^2$	N/A
Softmax Accuracy	0.792	Log likelihood	N/A

Table 8: Hardmax Confusion Matrix from Proposed Mode Choice Model

Obs\Pred	Active	Auto	Transit	Observed	Accuracy
Active	3116	13	676	3805	81.9%
Auto	41	81	1191	1313	6.2%
Transit	360	66	8813	9239	95.4%
Predicted	3517	160	10680	14357	83.7%

Table 9: Softmax Confusion Matrix from Proposed Mode Choice Model

Obs\Pred	Active	Auto	Transit	Observed	Accuracy
Active	2827.7	32.7	944.6	3805	74.3%
Auto	36.2	269.0	1007.8	1313	20.5%
Transit	304.2	662.5	8272.4	9239	89.5%
Predicted	3168.1	964.1	10224.8	14357	79.2%

As can be seen, the accuracy of the mode choice model is quite good. For reference, a model with only alternative-specific constants would result in a hardmax accuracy of 62.7% (the market share of Transit) and softmax accuracy of 46.6% (the sum of the squares of the market shares). This mode choice model is used in the next section to examine the impact of using a more detailed measure of school location accessibility in the PS location choice problem.

### 6.2.5 Results

The accessibility model which includes the mode choice model as shown in [5] is compared with the distance model developed previously. Table 10 shows a comparison of these results. The accessibility model does not outperform the much simpler distance model. Meanwhile, the combination of both models offers a small improvement over the distance model.

Table 10: Comparison of Distance and Accessibility Models. \*\*\* indicates  $p < 0.001$ .

Parameter	Distance			Accessibility			Combined		
	Estimate	Std. Error		Estimate	Std. Error		Estimate	Std. Error	
$B_{OC}$	-1.648	0.043	***	-1.249	0.038	***	-1.382	0.041	***
$B_{RY}$	-2.525	0.049	***	-2.566	0.049	***	-2.514	0.049	***
$B_{SC}$	-0.749	0.023	***	-0.781	0.024	***	-0.748	0.024	***
$B_{SG}$	-1.423	0.037	***	-1.453	0.035	***	-1.396	0.037	***
$B_{YG}$	-2.812	0.058	***	-2.473	0.058	***	-2.589	0.059	***
$B_{YG}$	-0.520	0.024	***	-0.226	0.024	***	-0.340	0.025	***
$B_{Dist}$	-0.0834	0.001	***				-0.0490	0.002	***
$B_{Access}$				0.8413	0.014	***	0.4771	0.016	***
Metric									
Hardmax Accuracy	0.480			0.460			0.475		
Softmax Accuracy	0.330			0.345			0.352		
Log Likelihood	-19814			-19840			-19315		
McFadden R <sup>2</sup>	0.128			0.127			0.150		

### 6.3 Campus-specific Attributes

The next step in the logit model development involves integrating campus-specific attributes. The following attributes are considered: total enrollment, average first-year domestic tuition for the Arts and Science program, proportion of domestic enrollment in undergraduate programs, and secondary school admission averages. These values were obtained from 2015-16 data from [Common University Data Ontario \(CUDO\)](#). Table 11 summarizes the attributes for the seven campuses:

Table 11: Summary of Campus Attributes

School Code	Tuition (CAD)	Domestic Enrollment	Admission Average	Total Enrollment
SG	7519	80.8%	89.3%	53930
SC	7813	83.8%	84.1%	11770
MI	7670	82.8%	83.0%	13298
YK	7339	89.2%	81.7%	41142
YG	7339	89.2%	81.7%	2457
RY	7026	96.7%	84.0%	28159
OC	7052	90.0%	82.4%	3491

One objective in this analysis is to make the model generalizable to expanded choice sets, which requires avoiding alternative-specific constants and coefficients. Instead, these constants are replaced by the campus attributes described above. Upon expanding the choice set, such attributes can be included in the model directly. Table 12 presents the results for the selected model that includes campus attributes as described above. Key findings from this exercise are:

- Unlike many of the studies in the literature review, it was found that including tuition information did significantly improve the model. Even interacting tuition with household

income was not found to be effective. This result can be attributed to the minor differences between tuition fees for different GTHA schools.

- Domestic enrollment rate was found to be most useful when interacted with living arrangement. Presumably, students living with their family are more likely to be domestic, and hence attend a school with more domestic students.

Table 12: Location Choice Models with Campus Attributes. \*\*\* indicates  $p < 0.001$ .  $F_i = 1$  if the student lives with their family/parents, otherwise  $F_i = 0$ .

Parameter	Distance			Accessibility			Combined		
	Estimate	Std. Error		Estimate	Std. Error		Estimate	Std. Error	
$B_{Dist}$	-0.0843	0.0012	***				-0.0535	0.0016	***
$B_{Access}$				0.8176	0.0135	***	0.4389	0.0161	***
$B_{Log(Enrol)}$	0.8007	0.0144	***	0.8665	0.0146	***	0.8212	0.0146	***
$B_{Admission Ave}$	0.0743	0.0038	***	0.0279	0.0040	***	0.0489	0.0040	***
$F_i * B_{Domestic \%}$	0.0411	0.0021	***	0.0229	0.0021	***	0.0311	0.0022	***
Metric									
Hardmax Accuracy	0.476			0.455			0.479		
Softmax Accuracy	0.334			0.342			0.352		
Log Likelihood	-19654			-19840			-19235		

Interestingly, while the distance and combined models have generally improved, the accessibility has gotten less effective. It outperforms the distance model only on the softmax accuracy. Note, also, that the estimated parameters for admission average confirm previous findings that greater selectivity increases the attractiveness of schools.

#### 6.4 Socioeconomic Variables Interacted with Distance and Accessibility

Next, the addition of socioeconomic variables to the model is explored. While the interaction of socioeconomic variables with campus-specific attributes has already been tested, their interaction with distance and accessibility is explored here. Based on the differences in parameters from the Segmented Gravity Model, this addition is expected to be significant. After iterating through several trial specifications, Table 13 presents the results for the model with the best-performing specification.

It is seen that students living with their family are less sensitive to distance and accessibility than their non-family counterparts. Also, students working full-time are less sensitive to accessibility, perhaps since they measure the accessibility of their school location with respect to their workplace rather than their place of residence. A similar effect is observed to a lesser extent for part-time workers.

Table 13: Socioeconomic Variables in Location Choice Models. \*\*\* indicates  $p < 0.001$ .  $F_i = 1$  if the student lives with their family/parents, otherwise  $F_i = 0$ .  $W_i = 1$  if the student works full-time, otherwise  $W_i = 0$ .  $P_i = 1$  if the student's enrollment status is part-time, otherwise  $P_i = 0$ .

Parameter	Distance			Accessibility			Combined		
	Estimate	Std. Error		Estimate	Std. Error		Estimate	Std. Error	
$B_{Dist}$	-0.1231	0.002	***				-0.0736	0.003	***
$B_{Access}$				0.8176	0.014	***	0.4468	0.021	***
$B_{Log(Enrol)}$	0.8043	0.014	***	0.8665	0.015	***	0.8115	0.014	***
$B_{Admission Ave}$	0.0567	0.004	***	0.0279	0.004	***	0.0476	0.004	***
$F_i * B_{Domestic \%}$	0.0327	0.002	***	0.0229	0.002	***	0.0298	0.002	***
$F_i * B_{Dist\_Family}$	0.0589	0.003	***				0.0153	0.004	***
$F_i * B_{Access\_Family}$							-0.3020	0.043	***
$W_i * B_{Access\_Work}$							-0.4667	0.100	***
$P_i * B_{Access\_PT}$							-0.2288	0.053	***
Metric									
Hardmax Accuracy	0.4803			0.4552			0.4807		
Softmax Accuracy	0.3435			0.3416			0.3550		
Log Likelihood	-19406			-19840			-19133		

## 6.5 Closest School Dummies

Table 14: Closest Dummies in Location Choice Models. \*\*\* indicates  $p < 0.001$ .  $F_i = 1$  if the student lives with their family/parents, otherwise  $F_i = 0$ .  $W_i = 1$  if the student works full-time, otherwise  $W_i = 0$ .  $P_i = 1$  if the student's enrollment status is part-time, otherwise  $P_i = 0$ .

Parameter	Distance			Accessibility			Combined		
	Estimate	Std. Error		Estimate	Std. Error		Estimate	Std. Error	
$B_{Dist}$	-0.1043	0.002	***				-0.0832	0.003	***
$B_{Access}$				0.8663	0.018	***	0.2671	0.028	***
$B_{Closest}$	0.9287	0.042	***	-0.2310	0.053	***	0.5444	0.060	***
$B_{Log(Enrol)}$	0.8011	0.014	***	0.8660	0.015	***	0.8058	0.015	***
$B_{Admission Ave}$	0.0599	0.004	***	0.0261	0.004	***	0.0539	0.004	***
$F_i * B_{Domestic \%}$	0.0331	0.002	***	0.0223	0.002	***	0.0315	0.002	***
$F_i * B_{Dist\_Family}$	0.0414	0.003	***				0.0214	0.004	***
$F_i * B_{Access\_Family}$							-0.2185	0.043	***
$W_i * B_{Access\_Work}$							-0.4222	0.098	***
$P_i * B_{Access\_PT}$							-0.2142	0.052	***
Metric									
Hardmax Accuracy	0.4646			0.4537			0.4734		
Softmax Accuracy	0.3540			0.3414			0.3565		
Log Likelihood	-19154			-19831			-19091		

The final addition to the location choice model is including “closest school dummies”  $C_{ij}$ , representing which school is closest to the student’s home zone. That is,  $C_{ij} = \{1 \text{ if } d_{ij} \leq$

$d_{ik} \forall k \neq j$ , else 0}. Moreover, it is hypothesized that the closest school dummies are most meaningful for schools within a certain distance of the student's home zone. Upon experimenting with this maximum distance, a threshold of 2km is chosen, such that  $C_{ij} = \{1 \text{ if } d_{ij} \leq 2\text{km and } d_{ij} \leq d_{ik} \forall k \neq j, \text{ else } 0\}$ .

Table 14 presents the results for all three models when these closest dummies are incorporated. It is seen that the distance model performs almost as well as the combined model, despite including much fewer variables (recall that the accessibility term includes a non-trivial mode choice model). Furthermore, the accessibility model performs quite poorly relative to the other models. Due to this effectiveness and the relative simplicity of the distance model, this model is selected as the preferred one. Notice that the parameter for the closest school dummy is positive and significant, as would be expected.

### 6.6 Proposed Model

Given the analyses and discussion presented in the previous sections, the proposed logit model for school location choice is:

$$V_{ij} = B_{Enrol} * \log(E_j) + B_{AdmAve} * AA_j + B_{Dom\%} * D_j * F_i + d_{ij} * B_{Dist} + B_{Dist\_Family} * F_i * d_{ij} + B_{Closest} * C_{ij} \quad [6]$$

where:

- $V_{ij}$  is the systematic utility for student  $i$  and campus  $j$ ,
- $E_j$  is the total enrollment of campus  $j$ ,
- $AA_j$  is the mean secondary school admission average for campus  $j$ ,
- $D_j$  is the domestic enrollment rate for undergraduate programs at campus  $j$ ,
- $F_i = \{1 \text{ if student } i \text{ lives with their family/parents, } 0 \text{ otherwise}\}$ ,
- $d_{ij}$  is the network distance between student  $i$ 's home zone and campus  $j$ ,
- $C_{ij} = \{1 \text{ if } d_{ij} \leq 2\text{km and } d_{ij} \leq d_{ik} \forall k \neq j, 0 \text{ otherwise}\}$ , and
- $B_{Enrol}$ ,  $B_{AdmAve}$ ,  $B_{Dom\%}$ ,  $B_{Dist}$ ,  $B_{Dist\_Family}$ , and  $B_{Closest}$  are estimated parameters.

The estimated parameters and metrics for this model are those reported for the "Distance" model in Table 14. Confusion matrices for this model are presented in Tables 15 and 16.

Table 15: Hardmax Confusion Matrix for Proposed Logit Location Choice Model

Obs\Pred	MI	OC	RY	SC	SG	YG	YK	Observed	Accuracy
MI	404	0	8	0	339	0	179	930	43.4%
OC	27	0	53	6	273	0	96	455	0.0%
RY	194	0	318	36	1431	0	729	2708	11.7%
SC	6	0	18	184	639	0	227	1074	17.1%
SG	239	0	529	53	4256	0	834	5911	72.0%
YG	13	0	8	3	203	0	88	315	0.0%
YK	172	0	54	30	1264	0	1564	3084	50.7%
Predicted	1055	0	988	312	8405	0	3717	14477	46.5%

Table 16: Softmax Confusion Matrix for Proposed Logit Location Choice Model

Obs\Pred	MI	OC	RY	SC	SG	YG	YK	Observed	Accuracy
MI	271.3	26.3	166.1	19.9	277.5	11.9	157.1	930	29.2%
OC	23.2	19.5	116.1	24.2	190.1	8.7	73.2	455	4.3%
RY	166.9	90.9	687.8	173.4	997.2	58.2	533.7	2708	25.4%
SC	18.3	29.5	224.7	247.6	329.0	31.9	192.9	1074	23.1%
SG	227.6	227.1	1375.2	250.4	2897.5	102.2	831.0	5911	49.0%
YG	15.4	9.7	71.0	22.1	114.7	10.7	71.4	315	3.4%
YK	176.4	86.8	595.3	169.3	1000.0	66.6	989.7	3084	32.1%
<b>Predicted</b>	899.0	489.8	3236.1	906.9	5806.1	290.1	2849.1	14477	35.4%

## 7 2015 SMT0 Location Choice – Random Forest

In developing the random forest (RF) location choice model socioeconomic variables (such as living arrangement and enrollment status) and geospatial variables (such as distances to the campuses) were tested. Due to the nature of RFs, passing in campus-specific information is unhelpful. Instead, the algorithm is expected to identify patterns related by campus-specific attributes implicitly.

### 7.1 Geospatial Variables

Since the meaning of different variables, and their relationships to other variables, are not inherently captured in the RF, a feature engineering process was used to identify the best format in which to input geospatial information. The following approaches were considered:

- Home zones (H): The student’s home zone passed directly
- Coordinates (C): The latitude and longitude of the student’s home zone’s centroid, normalized between 0 and 1
- Planning districts (P): The number of the planning district containing the student’s home zone (see [http://dmg.utoronto.ca/pdf/tts/2016/2016TTS\\_DataGuide.pdf](http://dmg.utoronto.ca/pdf/tts/2016/2016TTS_DataGuide.pdf))
- Distances (D): The distances between the student’s home zone and each campus
- Distance rank labels (L): One-hot encoded columns labeling the  $n^{\text{th}}$  closest school to student’s home zone
- Ranked distances (R): Columns labelled  $n$  containing the distance to the  $n^{\text{th}}$  closest school from the student’s home zone

For approaches D, L, and R, passing a subset of these columns was also considered. For approach D, passing in only three columns seemed sufficient. This finding can be explained by the fact that three distances is sufficient to pinpoint a student’s home location, so including more columns is superfluous. For approach L, the columns for SG, RY, and OC were combined because of these campuses’ geographic proximity.

The results for various approaches showed limited fluctuations, even for the HZ approach. Because many of these approaches include variables that are high-cardinality, it is hypothesized that the RF model is overfitting the data by identifying “patterns” on what is, essentially, a zone-by-zone basis.

The PD approach is used in future analysis, as this is a lower-cardinality variable that is less susceptible to overfitting, yet provides valuable information on what part of the region a student lives in. Approach L is kept for  $n = 1$ , as this variable improves the model but is unlikely to lead to overfitting.

## 7.2 Feature Selection

One benefit of RFs is that feature importances can be calculated and analyzed. These can be used to identify the most relevant features for the problem, a process known as feature selection. In this study's feature selection process, various individual and household characteristics were investigated. The most important variables were found to be: living arrangement, level of study, household income range, and employment status, while the closest school dummy for YG is least significant.

## 7.3 Hyperparameter Tuning

After selecting the model input format, the next step is hyperparameter tuning. A randomized search with cross-validation and then a grid search with cross-validation were used, as implemented by *sklearn*, to establish the best hyperparameter settings. However, the gains from this approach were marginal: the optimal parameters were very similar to the default parameters and only small changes in the performance metrics were seen.

## 7.4 Proposed Model

Table 17: Selected Random Forest Model. All features except PlanningDistrict are dummy variables. DT = Any downtown campus, YK = York Keele, MI = U of T Mississauga, SC = U of T Scarborough. PT = Part-time. Log likelihood, rho squared not reported since some observed choices are assigned a probability of 0.

Feature	Importance	Std. Dev
PlanningDistrict	42.99%	0.59%
LevelGrad	9.69%	0.11%
Family	8.12%	0.20%
Closest.DT	7.78%	0.46%
Closest.YK	5.91%	0.28%
StatusPT	4.00%	0.09%
WorkYes	3.80%	0.11%
IncomeLow	3.78%	0.12%
IncomeHigh	3.78%	0.06%
Closest.MI	3.54%	0.19%
Closest.SC	3.47%	0.13%
WorkNo	3.14%	0.11%
Metric	Testing Set	Training Set
Hardmax Accuracy	48.30%	58.07%
Softmax Accuracy	39.97%	46.69%

Table 17 shows the results and feature importances for the proposed RF model. The metrics reported are the model's average performance on a separate testing set across ten trials. The out-of-sample hardmax accuracy for the RF model is almost two percentage points higher than for the MNL model. This is unsurprising since the RF is trained so as to optimize the

hardmax accuracy. More interestingly, the RF out-of-sample softmax accuracy is over 4.5 percentage points better than for the proposed logit model. As such, the RF is outperforming the MNL model on both metrics. Tables 18 and 19 show the hardmax and softmax confusion matrices for the proposed model’s performance on the separate testing set.

*Table 18: Hardmax Confusion Matrix for Proposed Random Forest Location Choice Model*

Obs\Pred	MI	OC	RY	SC	SG	YG	YK	Observed	Accuracy
MI	133	0	30	0	42	0	45	250	53.2%
OC	14	0	27	6	54	3	11	115	0.0%
RY	58	0	164	50	237	6	122	637	25.7%
SC	4	1	63	111	49	0	48	276	40.2%
SG	61	1	167	45	1056	13	158	1501	70.4%
YG	2	0	16	8	25	5	14	70	7.1%
YK	50	0	105	41	249	0	326	771	42.3%
<b>Predicted</b>	322.0	2.0	572.0	261.0	1712.0	27.0	724.0	3620	49.6%

*Table 19: Softmax Confusion Matrix for Proposed Random Forest Location Choice Model*

Obs\Pred	MI	OC	RY	SC	SG	YG	YK	Observed	Accuracy
MI	80.0	5.9	47.8	4.2	56.1	5.8	50.2	250	32.0%
OC	7.4	5.0	27.1	8.2	45.0	3.6	18.7	115	4.3%
RY	42.6	22.9	163.8	47.4	222.0	16.4	121.9	637	25.7%
SC	4.9	8.4	57.2	83.1	61.2	7.0	54.2	276	30.1%
SG	52.3	45.3	240.4	68.3	826.5	27.5	240.6	1501	55.1%
YG	3.6	2.1	14.5	6.7	19.8	6.0	17.2	70	8.6%
YK	44.7	20.3	139.7	48.3	229.1	20.6	268.3	771	34.8%
<b>Predicted</b>	235.6	109.8	690.6	266.2	1459.8	86.9	771.1	3620	39.6%

## 8 2015 SMT0 Discussion

As discussed in previous sections, the performance of the proposed RF model is slightly superior to that of the logit model. This result suggests that machine learning techniques, and especially the RF algorithm, are tools that can be used effectively for the PS location choice problem. Further investigation and experimentation on this front is warranted, and would establish whether RFs are similarly effective in other discrete choice contexts. Despite the better performance of the RF model, it is arguable that there are several reasons why the logit model should be preferred for operational use.

[Breiman](#) (2001) notes that as the number of trees is increased, the RF avoids overfitting. Furthermore, [Segal](#) (2004) shows that hyperparameter tuning, such as restricting tree depth, the number of splits, or minimum node size for splits, can curb this effect. In this study, the use of high-cardinality variables (such as distances, coordinates, or home zone labels) is also avoided, instead opting for lower-cardinality features (planning districts), which further reduces the potential for overfitting. However, while these methods can address overfitting to the sample

data, the RF remains flawed when it comes to the model's generalizability. This flaw can be considered from two lenses: generalizing patterns from the sample to the entire student population, and generalizing the model to different contexts (such as for forecasting, or for a different choice set).

Firstly, sample bias may result in certain groups being under- or over-represented in the SMTO data. This would result in the RF making predictions based on relationships that do not accurately reflect the entire student population. For instance, if students attending campus  $j$  from a certain planning district have been oversampled, students from this planning district will consistently be assigned a higher-than-accurate probability of attending campus  $j$ . Hence, the RF model may not generalize effectively from the sample to the broader student population. While an elaborate weighting scheme could alleviate this issue, the creation of such a scheme would rely on more complete demographic information for different campuses, information that is not readily available.

The logit model is likely to be less sensitive to this issue. As a behavioural model, patterns in the sample are not "hard-wired" into the predictions in the same way as for the RF. This is especially true in this analysis given avoidance of the use of alternative-specific coefficients. Using the example above, while the over-sampling of students from said planning district to be attending campus  $j$  might suggest a more/less sensitive response to distance, this sensitivity will not greatly influence the parameter since the behaviours of all students in the sample are considered together.

Secondly, the RF model is not appropriate if the results are to be generalized to other contexts. The RF relies on patterns that exist in the sample, but cannot be effectively adapted to other contexts. For example, if the enrollment of a campus were to change significantly, the RF could not be used to effectively forecast college choice patterns. In contrast, enrollment is included as an alternative-specific variable in the logit model, so one would expect the logit model to be more generalizable.

In the case of changes in students' behavioural patterns, these observations cannot be inputted to the RF model. As a specific example, if a model for the future is predicted, and observations suggest that future students are less responsive to distance, this pattern cannot be conveyed to the RF algorithm, whereas for the logit model, a modified distance parameter can be imposed.

Furthermore, due to the nature of RF, such a model could not be used to generalize findings to a different choice set. In this analysis, one objective is to develop a model that would perform well on an expanded (more complete) choice set, such as that of the 2019 SMTO. This cannot be done with the RF. However, by excluding alternative-specific coefficients, such a generalization can be completed with the logit model. Below, it is shown that this generalization actually performs quite well when generalizing the logit model from the 2015 SMTO to the 2019 SMTO.

For all these reasons, subsequent analysis focuses on the logit model approach.

## 9 2019 SMTO Location Choice – Logit Model

### 9.1 Imputing Enrollment

Total enrollment rates for different campuses are an important component of the proposed location choice model. [Ontario's Open Data Team](#) (2019) provides data containing enrollment

totals by campus for Ontario’s colleges. However, these statistics do not correspond one-to-one with the colleges listed by 2019 SMTO respondents. Furthermore, this survey includes several university campuses for which enrollment totals are not available. Given this, enrollment totals for the missing campuses must be imputed if the model is to be applied to the 2019 data.

A simple gravity model was developed to accomplish this imputation. The log of enrollment is used as the attraction term for campuses where this is known. For the remaining campuses, alternative-specific constants are estimated. These constants are then exponentiated to obtain estimated enrollments. In effect, the sampling rates for each campus are used to impute the total student population. For some campuses, the results obtained by this method seemed reasonable. However, in some cases the predictions were clearly the wrong order of magnitude. For these schools, the total enrollment across all of the institution’s campuses was known. Thus, it was assumed that the relative sampling rates from each campus reflect the proportion of students enrolled at each, and calculated enrollment by campus by multiplying the institution’s total enrollment by these proportions. While these imputed enrollments provide reasonable grounds upon which to continue the analysis, more accurate information should be obtained to improve the model’s quality.

## 9.2 Initial Results

The first step for the 2019 SMTO analysis, is to estimate an MLN model using the same formulation as for the 2015 dataset and compare the results. Since domestic enrollment rate and admission averages are not available for many campuses, these variables have been removed from the model. Hence, the modified utility function used is:

$$V_{ij} = B_{Enrol} * \log(E_j) + d_{ij} * B_{Dist} + B_{Dist\_Family} * F_i * d_{ij} + B_{Closest} * C_{ij} \quad [7]$$

where:

- $V_{ij}$  is the systematic utility for student  $i$  and campus  $j$ ,
- $E_j$  is the imputed or known total enrollment of campus  $j$ ,
- $d_{ij}$  is the network distance between student  $i$ ’s home zone and campus  $j$ ,
- $F_i = \{1 \text{ if student } i \text{ lives with their family/parents, } 0 \text{ otherwise}\}$ ,
- $C_{ij} = \{1 \text{ if } d_{ij} \leq 2\text{km and } d_{ij} \leq d_{ik} \forall k \neq j, 0 \text{ otherwise}\}$ , and
- $B_{Enrol}$ ,  $B_{Dist}$ ,  $B_{Dist\_Family}$ , and  $B_{Closest}$  are estimated parameters.

Table 20: Initial Model Results for 2019 SMTO. \*\*\* indicates  $p < 0.001$ . Errors and significances for 2015 Parameters are for the 2015 dataset.

Parameter	2019 Parameters			2015 Parameters		
	Estimate	Std. Error		Estimate	Std. Error	
$B_{Dist}$	-0.0113	0.0004	***	-0.1089	0.0024	***
$B_{Log(Enrol)}$	0.9249	0.0081	***	0.8991	0.0121	***
$B_{Closest}$	2.4371	0.0386	***	0.9042	0.0413	***
$B_{Dist\_Family}$	-0.0023	0.0006	***	0.0507	0.0027	***
Metric						
Hardmax Accuracy	0.2645			0.3302		
Softmax Accuracy	0.1763			0.2418		
Log Likelihood	-38558.5			-53807.0		

Table 20 presents estimation results for two versions of this model: one with parameters estimated so as to maximize the log-likelihood for the 2019 dataset, and one with the parameters as estimated with the 2015 dataset.

At this point, there are three noteworthy observations. Firstly, the 2015 parameters lead to better classification accuracies than the 2019 parameters, although they do not maximize log-likelihood. This result suggests that the log-likelihood is heavily swayed by the least likely observations. While such observations cannot be ignored, the quality of a model should not be dictated primarily by these.

Secondly, the distance parameter has significantly decreased in magnitude for the 2019 parameters. Instead, the closest-school parameter has significantly increased in magnitude. While this may represent a change in the importance of distance in students' decision-making process, it is also possible that this change is misleading. Due to the larger set of included campuses in the 2019 dataset, and associated greater geographic spread, it is possible that some students attend very distant schools (for example if they indicated their permanent address as their home location, rather than the location from which they commute to school). This could drive the distance parameter to be smaller in magnitude, so as to improve log-likelihood. Future work could seek to identify such outliers in the data and re-estimate this model to gain a better understanding of how the relevance of distance has changed.

Thirdly, the sign for  $B_{Dist\_Family}$  has changed. According to the 2019 parameters model, students living with their family/parents are more responsive to distance than other students. This result is surprising, and may be influenced by response bias, as the 2019 dataset has a much lower response rate for living arrangement.

A more apt comparison of the trends in the 2019 and 2015 datasets can be made by estimating a model only on students attending the seven campuses from the 2015 dataset.

### 9.3 Subset Results

Table 21 shows the results for the location choice model with three datasets: the full 2015 dataset, the subset of the 2019 dataset containing students attending the seven campuses from the 2015 dataset, and a joint dataset with naïve pooling.

Table 21: Results of Proposed Model for Sample Subsets. \*\*\* indicates  $p < 0.001$ .

Parameter	2015			2019 Subset			Joint (naïve pooling)		
	Estimate	Std. Error		Estimate	Std. Error		Estimate	Std. Error	
$B_{Dist}$	-0.1089	0.0024	***	-0.0892	0.0020	***	-0.0927	0.0014	***
$B_{Log(Enrol)}$	0.8991	0.0121	***	0.8404	0.0132	***	0.8660	0.0089	***
$B_{Closest}$	0.9042	0.0413	***	1.0644	0.0474	***	1.0258	0.0316	***
$B_{Dist\_Family}$	0.0507	0.0027	***	0.0370	0.0028	***	0.0375	0.0018	***
Metric									
Hardmax Accuracy	0.4622			0.3840			0.4293		
Softmax Accuracy	0.3479			0.3069			0.3301		
Log Likelihood	-19307.1			-15560.4			-34801.3		
Mean loss	-1.334			-1.421			-1.369		

From these results, it is seen that the model performs better on the 2015 dataset than on the 2019 dataset. This is to be expected as the model formulation was developed using the former. Additionally, the family-distance interaction term is positive and significant in all three trials, suggesting a consistent pattern differentiating the behaviours of students with different living arrangements. Finally, note that the magnitude of the distance parameter has decreased for the 2019 model. However, this happens to a much smaller extent than above, suggesting that the drastic change in the distance parameter above is therefore not representative of the entire sample. Instead, it is possible that the addition of more campuses outside Toronto has influenced the distance parameter. Another possible contributing factor is that distance is perceived differently by students attending college rather than university. As such, the next step is to see if this distinction can be usefully introduced into the model.

## 9.4 Distinguishing Between University and College Students

### 9.4.1 Nested Logit Model

The first, and perhaps most natural, approach to emphasize the distinction between college and university students is by implementing a nested logit (NL) model, where the university campuses are in one nest and the college campuses are in another. Table 22 presents the results for two NL formulations compared with the un-nested MNL

From these results, it is seen that the NL model with nesting by institution types is not effective. As such, a different approach to distinguish between university and college students is desired. In particular, two of the three scale parameters are greater than 1.0 in value (violating the assumed nesting structure) and the third is not statistically different from 1.0 in value at standard confidence levels.

Table 22: Results for Nested Model for 2019 Location Choice. A  $\mu > 1$  implies greater correlation across nests than within.

Parameter	Reference (Un-nested)			Nested – One Scale Param.			Nested – Two Scale Params.		
	Estimate	Std. Error		Estimate	Std. Error		Estimate	Std. Error	
$B_{Dist}$	-0.0113	0.0004	***	-0.0185	0.0005	***	-0.0139	0.0004	***
$B_{Log(Enrol)}$	0.9249	0.0081	***	1.2874	0.0198	***	0.8946	0.0245	***
$B_{Closest}$	2.4371	0.0386	***	3.6470	0.0835	***	2.6111	0.0769	***
$B_{Dist\_Family}$	-0.0023	0.0006	***	-0.0037	0.0006	***	-0.0021	0.0004	***
$\mu_{uni}$				1.6184	0.0336	***	1.1639	0.0282	***
$\mu_{col}$							0.9564	0.0357	***
Metric									
Hardmax Accuracy	0.2645			0.2473			0.2474		
Softmax Accuracy	0.1763			0.1786			0.1772		
Log Likelihood	-38558.5			-38277.2			-38261.1		

### 9.4.2 Random Forest Classifier

Having seen the effectiveness of machine learning techniques in classifying living arrangement, a RF model to classify students according to their institution type was developed. Since this is a binary classification task, and there are fewer college students with respect to university students

in the sample, the College F-1 score is optimized. This is calculated as follows, with “College” as the positive class:

$$F_1 = \frac{2 * Precision * Recall}{Precision + Recall}$$

where:

$$Precision = \frac{TP}{TP + FP}$$

$$Recall = \frac{TP}{TP + FN}$$

and

*TP = True Positives*  
*FP = False Positives*  
*FN = False Negatives*

Table 23 presents the feature importances for the selected model. This model has an F1 score of 0.4447. Table 24 shows the confusion matrix for the model on a separate testing set. Figure 2 shows the receiver-operator curve for the model. The area under the curve is 0.7697.

Table 23: Feature Importances for Selected Random Forest School Type Classifier. All features except PlanningDistrict and Age are dummy variables. ClosestUni is 1 if the student’s home zone is closest to a university campus, 0 otherwise.

Feature	Importance
PlanningDistrict	44.32%
Age	34.25%
ClosestUni	5.50%
IncomeLow	2.85%
FamilyTrue	1.90%
LicenceFalse	1.85%
FamilyFalse	1.83%
Cars2+	1.69%
IncomeHigh	1.58%
LicenceTrue	1.48%
Cars1	1.45%
Cars0	1.30%

Table 24: Confusion Matrix for School Type Classifier

Obs\Pred	College	University	Observed	Accuracy
College	348	535	883	39.4%
University	334	3009	3343	90.0%
Predicted	682	3544	4226	79.4%

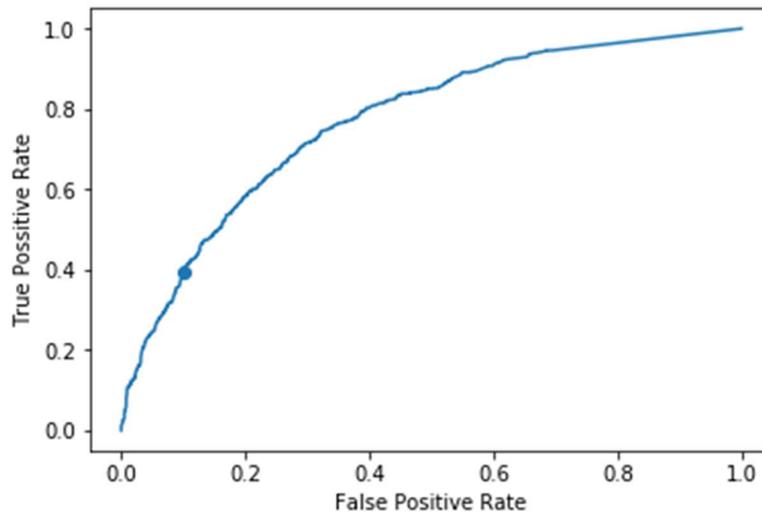


Figure 2: Receiver-Operator Curve for School Type Classifier. The point shown is that associated with a threshold of 50%.

A better F1 score can be obtained by adjusting the probability threshold at which students are predicted to be college students. Indeed, after reducing this threshold, an F1 score of 0.4998 was obtained. Table 25 presents the confusion matrix for this updated model.

Table 25: Confusion Matrix for School Type Classifier with Selected Threshold

Obs\Pred	College	University	Observed	Accuracy
College	2632	711	3343	78.7%
University	352	531	883	60.1%
Predicted	2984	1242	4226	74.8%

### 9.4.3 Separate Models for University and College Choice

It was hoped that the model can be improved by assigning students to separate university choice and college choice models according to their predicted institution type. To test this, separate models were estimated using the two subsamples. In evaluating this model's performance, the RF model was used to assign students to the appropriate school category. The results are presented in Table 26.

From this table, it is seen that the idea of developing separate location choice models by school type, combined with modelling school type allocation is promising when it comes to hardmax accuracy but does not lead to any gains for softmax accuracy. In particular, the college model suffers from very low softmax accuracy, although this is impacted by the fact that about one-third of the students who are assigned to this model do not actually attend a college. Given these poor results, the analysis reverted to the unified model and tried to incorporate the RF predictions in different ways.

Table 26: Results for 2019 Location Choice Separated by School Type. Note that log-likelihood is not predicted as any misclassified students will contribute a log likelihood of negative infinity. Also note that the family-distance interaction term was removed as it was statistically insignificant in both models.

	University Choice			College Choice		
University Students	11841			1207		
College Students	986			2482		
Total Sample	12827			3689		
Parameter	Estimate	Std. Error		Estimate	Std. Error	
$B_{Dist}$	-0.0113	0.0004	***	-0.1089	0.0024	***
$B_{Log(Enrol)}$	0.9249	0.0081	***	0.8991	0.0121	***
$B_{Closest}$	2.4371	0.0386	***	0.9042	0.0413	***
Metric						
Hardmax Accuracy	0.3130			0.3833		
Softmax Accuracy	0.2085			0.0473		
Weighted Average						
Hardmax Accuracy	0.3287					
Softmax Accuracy	0.1725					

#### 9.4.4 Including Random Forest Probabilities and Predictions

The addition of several terms to the utility function was experimented with:

- $P_{Col}$ : The RF-generated probability that the student is a college student, included in the utility function for colleges only.
- $P_{Uni}$ : The RF-generated probability that the student is a college student, included in the utility function for universities only.
- $P_{Type}$ : The RF-generated probability that the student attends a school of the alternative's type, included for all schools.
- $Pred\_Type$ : A dummy variable that equals 1 if the student is predicted to attend a school of the alternative's type (using the optimal threshold from above) and 0 otherwise.

The results for various combinations of these terms are shown in Tables 27 and 28. These models generally offer a reasonable improvement over the reference model for both hardmax and softmax accuracies, and log likelihood. However, a degree of skepticism should be used when considering these results, as many of the students in the data were used to train the RF model, making the probabilities and predictions likely more accurate than they would be for the entire population. It seems that more work is warranted to better establish a student's institution type. For instance, one idea which has not yet been explored is assigning students which the RF is fairly confident attend a university to the separate university model but using the full model for other students.

Table 27: Parameters for Models with Random Forest Predictions and Probabilities

	$B_{Dist}$	$B_{Log(Enrol)}$	$B_{Closest}$	$B_{Dist\_Family}$	P_Col	P_Uni	P_Type	Pred_Type
Reference	-0.0113	0.9249	2.4371	-0.0023				
P_Col	-0.0103	1.1063	2.3362	-0.0024	2.6037			
P_Uni	-0.0109	0.7139	2.3335	-0.0021		1.4250		
P_Type	-0.0102	0.7391	2.2201	-0.0021			2.5745	
P_Col + P_Uni	-0.0099	0.8225	2.1983	-0.0021	3.9158	2.2766		
Pred_Type	-0.0102	0.8281	2.2473	-0.0022				1.4739

Table 28: Performance Metrics for Models with Random Forest Predictions and Probabilities

	Hardmax Accuracy	Softmax Accuracy	Log Likelihood
Reference	26.45%	17.63%	-38558.5
P_Col	30.41%	19.15%	-37380.3
P_Uni	24.99%	18.16%	-37471.8
P_Type	28.49%	19.58%	-35832.0
P_Col + P_Uni	30.52%	20.06%	-35521.9
Pred_Type	30.84%	19.55%	-36265.2

## 10 2019 SMTO Discussion

The model remains somewhat ineffective once the more diverse choice set for the 2019 SMTO dataset is introduced. One significant limiting factor seems to be identifying students' institution type. From experience, it seems that students largely consider only one institution type in their choice sets, so eliminating irrelevant alternatives could lead to significant improvements in the model's performance. Previous studies have shown such variables as academic performance, ethnic background, and participation in extracurricular activities in high school to be useful indicators for students' selected institution type. Unfortunately, these variables are unavailable in this study.

It is also observed that maximizing log likelihood does not necessarily correspond with gains in other performance metrics, and can lead to estimated models which perform quite poorly on other metrics. Particularly, the parameters estimated for the 2019 model result in significantly lower classification accuracies than those from the 2015 model. This finding demonstrates a flaw in maximizing log likelihood in such cases. The maximization is weighed towards the most unlikely observations and hence might not effectively capture the model's holistic performance. Possibly, this problem only persists in unbalanced datasets, as is the case here. It is noted that it is possible to greatly reduce this effect by using only a subset of the data with a smaller, more balanced, choice set. In this study, a model on the subset of students attending schools included in the 2015 survey is estimated. However, doing so is an oversimplification of the problem at hand, especially as it would likely be difficult to effectively classify individuals according to whether or not they attend a school in this subset.

## 11 Future Work

Several avenues for future work that would build upon the analysis presented in this report are briefly described below.

**Generalization to TTS and Implementation in GTAModel:** This project was undertaken with the hope of eventual implementation of the developed model within [GTAModel](#). As such, creating a model that can be generalizable to an expanded choice set is critical. This necessitates avoiding the use of alternative-specific coefficients in the logit model. However, it remains to be seen whether this approach can lead to solid results in a more generalized setting or not. One way to test this is by using data from the TTS to verify the performance of the model. An associated challenge is that the set of postsecondary institutions is much larger, and includes several smaller, specialized institutions. Using these data to adapt the model will allow for a final product to be developed that can be implemented effectively in GTAModel.

**Adjusting Enrollments by Level of Study:** In this study, the location choice sets of students are not restricted in any way. However, if school choice sets could be constrained effectively model accuracy would likely improve. One way to constrain choice sets is by modelling the admissions process. A simple admissions model, such as the one used by Kohn et al. (1974) or [Montgomery \(2002\)](#), can be implemented and its effects on model performance observed.

**Modelling Choice Sets:** While the SMTO data includes participants' level of study (i.e. undergraduate vs. graduate), this variable was not used as it is not available in the TTS survey. However, adjusting the campus enrollments according to the student's level of study would likely yield significant improvements to the model's performance. This is because several campuses have much smaller populations of graduate students compared to undergraduates. In fact, from the RF model it is seen that level is indeed an important variable in the classification. If a model can be successfully trained to classify students according to their level of study (as has been done with living arrangement) given such variables as age, income, employment status, living arrangement, etc., then enrollment level can and should be included in the analysis.

**Exploration of Random Forest and Machine Learning Techniques:** One noteworthy finding from this study was the effectiveness of the random forest classifier algorithm relative to the logit model. While using random forests comes with associated concerns, as discussed above, this foray into the realm of machine learning reveals that there is promising potential to use such techniques in PS location choice problems, and possible other discrete choice modelling applications. Further work in this area could lead to novel approaches being used in the field.

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